

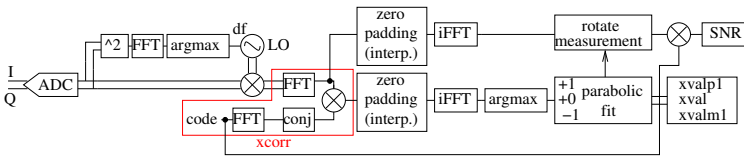


Considering the tremendous increase in computational power, an investigation on the various code lengths has shown [4] no impact on the time transfer stability, the improved SNR brought by the increased pulse compression ratio associated with long codes being compensated for by the fewer averages with a given exchange sequence. We have selected a 100 kchip-long code at a rate of 2.5 Mchips/s in order to reduce the Pulse Repetition Interval (PRI) and hence the range uncertainty since delays on a baseline as wide as Western Europe exceed the 4 ms PRI of the 10 kchip-long SATRE code. We have selected 17-bit long maximum-length sequence Galois-field PRN sequences with arbitrary seeds 09 and 15 for generating orthogonal codes. Increasing the PRI does reduce the digital communication datarate though, with the SATRE communicating 250 bits/s HiRate data whereas our implementation is limited to 25 bits/s holding the NTP second encoded as 8-bit binary format, least significant bit first after a start bit.

### 3 Link budget and signal to noise ratio

Various link budget indicators are needed, with most commonly the received signal power and SNR. While the total received signal power is the variance of the  $I + jQ$  datastream, this information is irrelevant in the case of CDMA communication when multiple emitters broadcast on the same carrier frequency. Hence, individual transmitted code identification is needed to assess the link budget with each transmitting station. The objective of the processing sequence is to extract the signal component of each code using the following algorithm (Fig. 2):

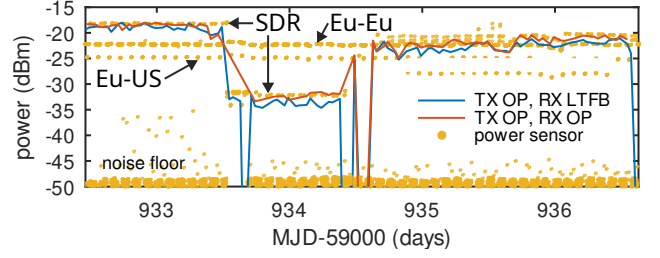
1. the time delay between the local copy of the code and the received signal is computed from the cross-correlation, possibly with some oversampling to identify the delay with sub-sampling period resolution
2. the local copy of the code is rotated by the resulting time delay and the received signal multiplied with this binary sequence, resulting in spectrum de-spreading by cancelling the BPSK modulation
3. the signal is the square of the mean value of the de-spread signal
4. the noise is the variance of the despread signal.



**Figure 2.** Outline of the signal processing algorithm on the receiver module.

We assess the SNR computation by comparing this quantity computed at the remote end of the link, on the receiver module, with the output power measurement as observed

by a microwave sensor on the emitter module. Excellent agreement is observed between the two quantities (Fig. 3).



**Figure 3.** Comparison of the SDR power estimate (blue, red in two-way and ranging measurements) with respect to a reference microwave power sensor located at the input port of the transmitting parabola at LNE-SYRTE (OP).

In the context of SDR, the objective is to get rid of unstable analog components to rely solely on reproducible and deterministic digital signal processing. Nevertheless, due the discrete time emitted signal generation, unwanted spectral components are generated from the Digital to Analog Converter (DAC) which are filtered at the output of the General Purpose Input/Output (GPIO) pin of the FPGA before feeding the microwave upconverter and amplifier for broadcasting to the geostationary satellite. SAW filters have been selected to efficiently ( $> 50$  dB) unwanted spectral components with insertion losses ( $\leq 25$  dB) low enough to keep the generated signal above the targeted level of  $-20$  dBm as typically generated by the SATRE modem to feed the VSAT emitter.

SAW filters being based on the conversion of electromagnetic waves to acoustic waves propagating on piezoelectric substrates prone to thermal drift, the impact of this analog components on the link delay must be assessed. Two filters were selected, C-Tech 321823 and SAWTEK 851547, both documented as 70 MHz IF bandpass filter with 2.5 MHz bandwidth. Both filters exhibit similar insertion losses (21.5 dB and 25.2 dB nominal losses respectively) but their temperature behavior and group delay are different. The former filter manufactured on lithium tantalate exhibits a nominal  $4.9 \mu\text{s}$  group delay with a temperature sensitivity of 20 ppm/K while the former is documented to exhibit a  $2.3 \mu\text{s}$  group delay and undocumented temperature sensitivity but its design on a quartz substrate would be compatible with a turnover temperature at room temperature and hence negligible first order temperature sensitivity. In all cases the time delay introduced by the SAW filter is expected to be in the picosecond range under the controlled environmental conditions of a TWSTFT setup, but with variations documented from filter to filter to be in the tens of nanoseconds.

### 4 Digital signal processing

The core concept of time transfer is cross correlation  $xcorr$ , and its practical implementation through the Fast Fourier

Transform  $FFT$  following the application of the convolution theorem stating that  $FFT(xcorr(x,y)) = FFT(x) \cdot FFT^*(y)$  for matching the pseudo random sequence  $x$  locally generated and the remote signal  $y$ . Extending the code duration for improving the SNR requires expanding computational capability as the load of a Fast Fourier Transform on  $N$  samples rises as  $N \log_2(N)$ .

We have selected a post-processing approach running on generic processing hardware (e.g. not requiring dedicated GPU hardware) in order to identify all communicating stations with no restriction on the number of channels processed during each session.

Digital signal processing holds the promises of reproducible results since digital algorithm execution is independent on environmental conditions (analog processing) or implementation. Despite floating point number description being inaccurate, the various proposed implementations in GNU/Octave, Python using FFTW or Numpy, and C++ all match to better than the 10th decimal or the hundred of ps.

## 5 Time and Frequency Transfer results

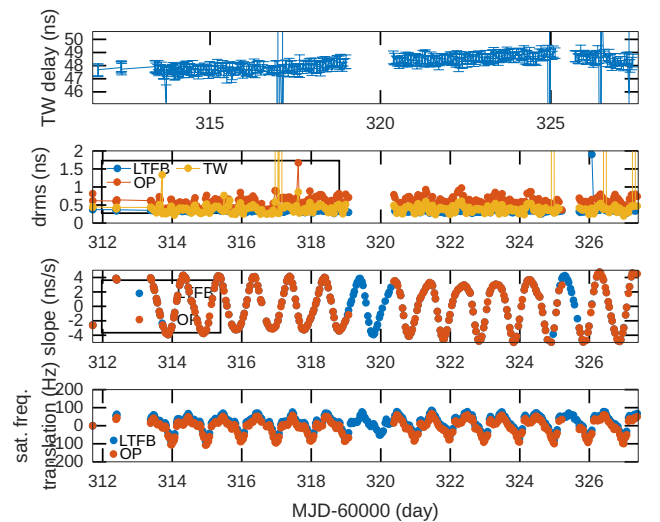
A two-week long TWSTFT session was completed using the same hardware setup located at LNE-SYRTE (OP) and LTFB. In both setups, the Artix-7 FPGA is clocked by the reference input 1-PPS and 10 MHz, with a PLL generating the 280 MHz signal clocking the PRN generator and the 70 MHz carrier spread by the BPSK modulation. Two Basic RX daughter boards with only a balun and no active frequency shifting are fitted on Ettus Research X310 receivers. The two channels are used on the one hand to collect on the reference channel the 70 MHz signal driving the upconverter as a loopback reference signal, and on the other channel the 70 MHz signal received by the downconverter.

Ranging and two-way signals have been collected and each correlation peak is timestamped on each reception site. The two-way analysis requires that the difference computation on the remote signal to loopback time difference computed at each end is performed at the same time so that the satellite motion contribution is cancelled. Because we have selected post-processing, the data storage is plagued by uncontrolled latencies including digital communication over Ethernet and file storage under supervision of a general purpose multitasking operating system with measurement sequences triggered by a mechanism – crontab – with poor timing resolution. The PRN synchronization on both link ends has been solved by using a single board Raspberry Pi 4 computer to actively probe the 1-PPS reference input on the one hand, and NTP synchronized to better than 1-second its real time clock. By detecting the rising edge of the 1-PPS prior to the start of the next communication session, the FPGA emission is enabled but only starts on the next rising edge of the 1-PPS. Under the assumption that the 1-PPS reference signal between both stations is aligned to

better than a few milliseconds, the satellite motion of a few ns/s induces a TWSTFT processing error in the picosecond range, negligible in the current application.

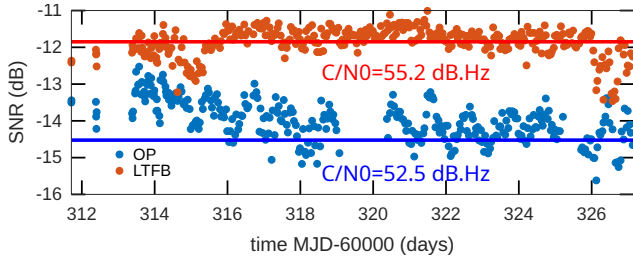
Figure 4 summarizes the result of a two-week TWSTFT measurement performed during the odd UTC hours between min 4 to min 9 and min 46 to min 51, each session lasting 5 minutes. From top to bottom:

1. the uncalibrated TWSTFT measurement ;
2. the standard deviation within each 5-minute long session of the remote communication after removal of the parabolic trend. The OP standard deviation is larger due to a weaker power feeding the loopback channel (−14 dBm), while the LTFB loopback gain was tuned to benefit from the full scale range of 6 dBm of the X310 analog to digital converter. In all cases the standard deviation within each 5-minute session remains below 1 ns ;
3. the satellite motion velocity as measured with the slope of the remote communication signal, emphasizing the need for synchronizing the two ends of the communication link to sub-100 ms to reach sub-nanosecond stability from one session to the next since the satellite motion can reach up to 4 ns/s ;
4. the frequency offset with respect to the nominal 70 MHz IF carrier, including the Doppler shift from the satellite motion and the satellite transponder frequency shift.



**Figure 4.** Two-week TWSTFT measurements between OP and LTFB using SDR emitter and receiver.

The SNR during these sessions is comparable with those classically exhibited by the SATRE modem, converted to a  $C/N_0$  value by adding the 67 dB of the 5 MHz channel bandwidth to reach values between 52 to 56 dB.Hz (Fig. 5).

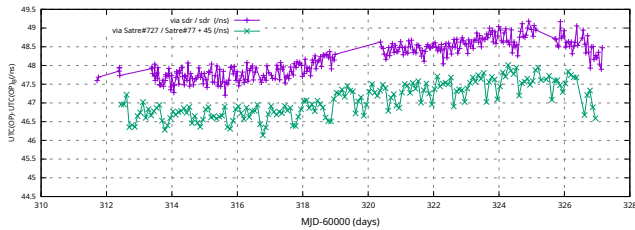


**Figure 5.** Signal to noise ratio at OP (blue) and at LTFB (red) during the same measurement session than displayed in Fig. 4.

## 6 Comparison between the SDR and SATRE TWSTFT

The Timetech SATRE modem is the TWSTFT reference instrument and the proposed solution is compared with the operational link between OP and LTFB. The SATRE communication is performed at the end of each UTC even hour while the SDR communication is performed at the beginning and end of each odd UTC hour. The SATRE communication lasts 3 minutes of which the last 2 minutes are used for TWSTFT analysis, while the whole 5 minute exchange of SDR is processed and used in the analysis.

The time-evolution of the comparison is exhibited in Fig. 6, with a close match of the observations by both instruments. The SDR link failed twice during the two-week sessions, in both cases with the X310 failing to transfer the expected number of samples to the recording GNU Radio script and the interface remaining busy during the subsequent link schedules.



**Figure 6.** Time evolution of the SDR TWSTFT link (purple) and SATRE link (green), offset to match the arbitrary time delay of the uncalibrated SDR measurement.

Detailed statistical analysis are currently underway.

## 7 Conclusion

We have demonstrated a functional, portable implementation of SDR emitter and receiver pairs for TWSTFT. Results on par with commercial proprietary hardware have been demonstrated, with an openhardware architecture targeted towards further improvements by the relevant communities. First results on the OP-LTFB link were presented, showing measurement fluctuations well below 500 ps over

several days and a signal to noise ratio in the 52 to 55 dB.Hz range.

As introduced, the proposed scheme is inspired by technology from the 1970s and 1980s with the use of the BPSK modulation for communicating through the satellite link. Global Navigation Satellite Systems (GNSS) have shifted to improved modulation schemes (BOC), improving spectral efficiency and improving digital communication performance using Forward Error Correction (FEC) whose investigation is perfectly suited to the opensource implementation of the TWSTFT platform. Further investigation will hence focus on improved modulation schemes and codes aimed at improving cross-code interference and timing resolution.

All software for reproducing the proposed setup is available at [https://github.com/oscimp/amaranth\\_twstft](https://github.com/oscimp/amaranth_twstft)

## Acknowledgements

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